



Mathematics (MEI)

Advanced Subsidiary GCE

Unit 4766: Statistics 1

Mark Scheme for January 2011

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by Examiners. It does not indicate the details of the discussions which took place at an Examiners' meeting before marking commenced.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the Report on the Examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Marking instructions for GCE Mathematics (MEI): Statistics strand

- 1. You are advised to work through the paper yourself first. Ensure you familiarise yourself with the mark scheme before you tackle the practice scripts.
- 2. You will be required to mark ten practice scripts. This will help you to understand the mark scheme and will not be used to assess the quality of your marking. Mark the scripts yourself first, using the annotations. Turn on the comments box and make sure you understand the comments. You must also look at the definitive marks to check your marking. If you are unsure why the marks for the practice scripts have been awarded in the way they have, please contact your Team Leader.
- 3. When you are confident with the mark scheme, mark the ten standardisation scripts. Your Team Leader will give you feedback on these scripts and approve you for marking. (If your marking is not of an acceptable standard your Team Leader will give you advice and you will be required to do further work. You will only be approved for marking if your Team Leader is confident that you will be able to mark candidate scripts to an acceptable standard.)
- 4. Mark strictly to the mark scheme. If in doubt, consult your Team Leader using the messaging system within *scoris*, by email or by telephone. Your Team Leader will be monitoring your marking and giving you feedback throughout the marking period.

An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

5. The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- 6. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- 7. The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

8. Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

Candidates are expected to give numerical answers to an appropriate degree of accuracy. 3 significant figures may often be the norm for this, but this always needs to be considered in the context of the problem in hand. For example, in quoting probabilities from Normal tables, we generally expect *some* evidence of interpolation and so quotation to 4 decimal places will often be appropriate. But even this does not always apply – quotations of the standard critical points for significance tests such as 1.96, 1.645, 2.576 (maybe even 2.58 – but not 2.57) will commonly suffice, especially if the calculated value of a test statistic is nowhere near any of these values. Sensible discretion *must* be exercised in such cases.

Discretion must also be exercised in the case of small variations in the degree of accuracy to which an answer is given. For example, if 3 significant figures are expected (either because of an explicit instruction or because the general context of a problem demands it) but only 2 are given, loss of an accuracy ("A") mark is likely to be appropriate; but if 4 significant figures are given, this should not normally be penalised. Likewise, answers which are slightly deviant from what is expected in a very minor manner (for example a Normal probability given, after an attempt at interpolation, as 0.6418 whereas 0.6417 was expected) should not be penalised.

However, answers which are *grossly* over- or under-specified should normally result in the loss of a mark. This includes cases such as, for example, insistence that the value of a test statistic is (say) 2.128888446667 merely because that is the value that happened to come off the candidate's calculator. Note that this applies to answers that are given as final stages of calculations; intermediate working should usually be carried out, and quoted, to a greater degree of accuracy to avoid the danger of premature approximation.

The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

9. Rules for crossed out and/or replaced work

If work is crossed out and not replaced, examiners should mark the crossed out work if it is legible.

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If two or more attempts are made at a question, and just one is not crossed out, examiners should ignore the crossed out work and mark the work that is not crossed out.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

10. Genuine misreading (of numbers or symbols, occasionally even of text) occurs. If this results in the object and/or difficulty of the question being considerably changed, it is likely that all the marks for that question, or section of the question, will be lost. However, misreads are often such that the object and/or difficulty remain substantially unaltered; these cases are considered below.

The simple rule is that *all* method ("M") marks [and of course all independent ("B") marks] remain accessible but at least some accuracy ("A") marks do not. It is difficult to legislate in an overall sense beyond this global statement because misreads, even when the object and/or difficulty remains unchanged, can vary greatly in their effects. For example, a misread of 1.02 as 10.2 (perhaps as a quoted value of a sample mean) may well be catastrophic; whereas a misread of 1.6748 as 1.6746 may have so slight an effect as to be almost unnoticeable in the candidate's work.

A misread should normally attract *some* penalty, though this would often be only 1 mark and should rarely if ever be more than 2. Commonly in sections of questions where there is a numerical answer either at the end of the section or to be obtained and commented on (eg the value of a test statistic), this answer will have an "A" mark that may actually be designated as "cao" [correct answer only]. This should be interpreted *strictly* – if the misread has led to failure to obtain this value, then this "A" mark must be withheld even if all method marks have been earned. It will also often be the case that such a mark is implicitly "cao" even if not explicitly designated as such.

On the other hand, we commonly allow "fresh starts" within a question or part of question. For example, a follow-through of the candidate's value of a test statistic is generally allowed (and

often explicitly stated as such within the marking scheme), so that the candidate may exhibit knowledge of how to compare it with a critical value and draw conclusions. Such "fresh starts" are not affected by any earlier misreads.

A misread may be of a symbol rather than a number – for example, an algebraic symbol in a mathematical expression. Such misreads are more likely to bring about a considerable change in the object and/or difficulty of the question; but, if they do not, they should be treated as far as possible in the same way as numerical misreads, *mutatis mutandis*. This also applied to misreads of text, which are fairly rare but can cause major problems in fair marking.

The situation regarding any particular cases that arise while you are marking for which you feel you need detailed guidance should be discussed with your Team Leader.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

11. Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

12. For answers scoring no marks, you must either award NR (no response) or 0, as follows:

Award NR (no response) if:

- Nothing is written at all in the answer space
- There is a comment which does not in any way relate to the question being asked ("can't do", "don't know", etc.)
- There is any sort of mark that is not an attempt at the question (a dash, a question mark, etc.)

The hash key [#] on your keyboard will enter NR.

Award 0 if:

- There is an attempt that earns no credit. This could, for example, include the candidate copying all or some of the question, or any working that does not earn any marks, whether crossed out or not.
- 13. The following abbreviations may be used in this mark scheme.
 - M1 method mark (M2, etc, is also used)
 - A1 accuracy mark
 - B1 independent mark
 - E1 mark for explaining
 - U1 mark for correct units
 - G1 mark for a correct feature on a graph
 - M1 dep* method mark dependent on a previous mark, indicated by *
 - cao correct answer only
 - ft follow through
 - isw ignore subsequent working

oe	or equivalent
rot	rounded or truncated
sc	special case
soi	seen or implied
WWW	without wrong working

14. Annotating scripts. The following annotations are available:

√and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working (after correct answer obtained)
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0,1
SC	Special case
٨	Omission sign
MR	Misread

Highlighting is also available to highlight any particular points on a script.

15. The comments box will be used by the Principal Examiner to explain his or her marking of the practice scripts for your information. Please refer to these comments when checking your practice scripts.

Please do not type in the comments box yourself. Any questions or comments you have for your Team Leader should be communicated by the *scoris* messaging system, e-mail or by telephone.

- 16. Write a brief report on the performance of the candidates. Your Team Leader will tell you when this is required. The Assistant Examiner's Report Form (AERF) can be found on the Cambridge Assessment Support Portal. This should contain notes on particular strengths displayed, as well as common errors or weaknesses. Constructive criticisms of the question paper/mark scheme are also appreciated.
- 17. Link Additional Objects with work relating to a question to those questions (a chain link appears by the relevant question number) see scoris assessor Quick Reference Guide page 19-20 for instructions as to how to do this this guide is on the Cambridge Assessment Support Portal and new users may like to download it with a shortcut on your desktop so you can open it easily! For AOs containing just formulae or rough working not attributed to a question, tick at the top to indicate seen but not linked. When you submit the script, *scoris* asks you to confirm that you have looked at all the additional objects. Please ensure that you have checked all Additional Objects thoroughly.
- 18. The schedule of dates for the marking of this paper is displayed under 'OCR Subject Specific Details' on the Cambridge Assessment Support Portal. It is vitally important that you meet these requirements. If you experience problems that mean you may not be able to meet the deadline then you must contact your Team Leader without delay.

	SECTION A			
Q1	Mode = 960 (grams)	B1 CAO		Ignore units and working
(i)	Median = 1020 (grams)	B1 CAO	2	
	N.B. 96 and 102 gets SC1			
(ii)	Positive	E1	1	Not right skewed
				Not positive correlation
		TOTAL	3	
Q2	$P(1) = \frac{13}{10} = \frac{13}{10} = 0.8125$	B1		Allow 0.813 or 0.812
(i)	$P(\text{product of two scores} < 10) = \frac{1}{16} = 0.8125$		1	
(ii)				
	P(even) × P(< 10) = 0.5 × $\frac{13}{16} = \frac{13}{32} = 0.40625$ P(even ∩ < 10) = $\frac{6}{16} = 0.375$ So not independent.	M1 for $0.5 \times \frac{13}{16}$ or $\frac{13}{32}$ FT their answer to (i) M1 for $\frac{6}{16}$ A1	3	Do not allow these embedded in probability formulae Also allow P(even <10) = $6/13 \neq P(even) = 1/2$ Or P(<10 even) = $6/8 \neq P(<10) = 13/16$ Or P(even <10) = $6/13 \neq P(even <10^{\circ}) = 2/3$ Or P(<10 even) = $6/8 \neq P(<10 even^{\circ}) = 7/8$ For all of these alternatives allow M2 for both probabilities. (M1 not available except if they correctly state both probabilities EG P(even <10) and P(even) and get one correct) If they do not state what probabilities they are finding, give M2 for one of the above pairs of probabilities with \neq symbol
		TOTAL	4	

Q3 (i)	$\begin{pmatrix} 13\\ 3 \end{pmatrix}$ ways of choosing the men = 286	M1 for $\begin{pmatrix} 13\\ 3 \end{pmatrix}$ seen A1	2	Accept ${}^{13}C_3$ or ${}^{13!}/_{(3!10!)}$ or equivalent for M1 No marks for permutations
(ii)	$\binom{13}{3} \times \binom{10}{3} = 286 \times 120 = 34320$	M1 for product A1 FT their 286	2	For permutations $1716 \times 720 = 1235520$ allow SC1 406 (from 286 + 120) scores SC1 (without further working)
(iii)	$\binom{23}{6} = 100947$ 34320/100947 = 1040/3059 = 0.340 (allow 0.34)	M1 for denominator of $\begin{pmatrix} 23 \\ 6 \end{pmatrix}$ A1 FT	2	FT their 34320 Or ${}^{6}C_{3} \times 13/23 \times 12/22 \times 11/21 \times 10/20 \times 9/19 \times 8/18 =$ 0.340 scores M1 for product of fractions and A1 for ${}^{6}C_{3} \times$ and correct evaluation For permutations 1235520/72681840=0.017 scores SC1 Allow full marks for fractional answers, even if unsimplified 406/100947 = 0.00402 gets M1A1 with or without working
		TOTAL	6	

Q4 (i)	$2k + 6k + 12k + 20k + 30k = 1, \ 70k = 1$ $k = \frac{1}{70}$	M1 A1 NB ANSWER GIVEN	2	For five multiples of k (at least four correct multiples) Do not need to sum or =1 for M1 Condone omission of either $70k = 1$ or $k = 1/70$ but not both Condone omission of k: $2+6+12+20+30=70$ Allow substitution of $k = 1/70$ into formula and getting at least four of $2/70$, $6/70$, $12/70$, $20/70$, $30/70$ for M1 and $2/70+6/70+12/70+20/70+30/70 = 1$ for A1
(ii)	$E(X) = 1 \times \frac{2}{70} + 2 \times \frac{6}{70} + 3 \times \frac{12}{70} + 4 \times \frac{20}{70} + 5 \times \frac{30}{70} = 4$ $E(X^{2}) = 1 \times \frac{2}{70} + 4 \times \frac{6}{70} + 9 \times \frac{12}{70} + 16 \times \frac{20}{70} + 25 \times \frac{30}{70} = \frac{1204}{70} = 17.2$ $Var(X) = 17.2 - 4^{2} = 1.2$	M1 for Σrp (at least 3 terms correct) A1 CAO M1 for $\Sigma r^2 p$ (at least 3 terms correct) M1dep for - their E(X) ² A1 FT their E(X) but not an error in E(X ²) provided Var(X) > 0	5	280/70 scores M1A0 USE of $E(X-\mu)^2$ gets M1 for attempt at $(x-\mu)^2$ should see $(-3)^2$, $(-2)^2$, $(-1)^2$, 0^2 , 1^2 (if $E(X)$ correct but FT their $E(X)$) (all 5 correct for M1), then M1 for $\Sigma p(x-\mu)^2$ (at least 3 terms correct with their probabilities) Allow all M marks with their probabilities, (unless not between 0 and 1, see below for all probs 1/70). Division by 5 or other spurious value at end gives max M1A1M1M1A0, or M1A0M1M1A0 if $E(X)$ also divided by 5. Unsupported correct answers get 5 marks. SC2 for use of 1/70 for all probabilities leading to E(X) = 3/14 and $Var(X) = 145/196 = 0.74$
		TOTAL	7	

Q5				Fractional answer = $7/25$ (Allow 28/100)
(i)	$P(Wet and bus) = 0.4 \times 0.7$	M1 for multiplying		
	= 0.28	probabilities	2	
		A1 CAO		
(ii)	P(Walk or bike) =	M1 for any two correct		$Or = 0.6 \times 0.9 + 0.4 \times 0.3$ gets M1 for either term
	$0.6 \times 0.5 + 0.6 \times 0.4 + 0.4 \times 0.2 + 0.4 \times 0.1$ or	pairs	3	= 0.54 + 0.12 gets M1 for sum of both
	0.3 + 0.24 + 0.08 + 0.04	M1 for sum of all four		
		correct terms		
		With no extra terms for		
		second MI		
	= 0.66	ALCAU		
				$Or = 1 - 0.6 \times 0.1 - 0.4 \times 0.7 = 0.66$. M1 for 1 - one
				A 1 for correct evaluation
(iii)	P(Dry given walk or bike) $-\frac{P(Dry and walk or bike)}{P(Dry and walk or bike)}$			
	$P(Walk \text{ or bike}) = \frac{P(Walk \text{ or bike})}{P(Walk \text{ or bike})}$	M1 for numerator		Allow 0.82, not 0.819 More accurate answer
	0.6×0.9 0.54 9 0.010	leading to 0.54	3	=0.81818 Fractional answer $= 54/66 = 27/33 = 9/11$
	===== 0.818	M1 for denominator		Condone answer of 0.8181
	0.00 0.00 11	Ft their P(Walk or bike)		Do not give final A1 if ans ≥ 1
		Irom (11) provided		
		between 0 and 1		
		ΑΙΓΙ		
		TOTAL	8	

Q6 (i)	(A) P(Avoided air travel) $=\frac{7}{100} = 0.07$ (B) P(At least two) $=\frac{11+2+1+4}{100} = \frac{18}{100} = \frac{9}{50} = 0.18$	B1 aef isw M1 for (11+2+1+4)/100 A1 aef isw	1 2	For M1 terms must be added must be as above or better with no extra terms (added or subtracted) for M1 Must simplify to $18/100$ or $9/50$ or 0.18 for A1 SC1 for $18/58$ Or $1 - (14+26+0+42)/100 = 0.18$ gets M1A1
(ii)	P(Reduced car use Avoided air travel) $=\frac{6}{7} = 0.857$	M1 for denominator 7 or 7/100 or 0.07 FT their (i)A A1 CAO	2	Allow 0.86
(iii)	P(None have avoided air travel) $=\frac{93}{100} \times \frac{92}{99} \times \frac{91}{98} = 0.8025$	M1 for 93/100× (triple product) M1 for product of remaining fractions A1	3	Fuller answer 0.802511, so allow 0.803 without working, but 0.80 or 0.8 only with working . $(93/100)^3$ scores M1M0A0 which gives answer 0.804357 so watch for this. M0M0A0 for binomial probability including 0.93 ¹⁰⁰ but ${}^{3}C_{0} \times 0.07^{0} \times 0.93^{3}$ still scores M1 $(k/100)^3$ for values of k other than 93 scores M0M0A0 $\frac{k}{100} \times \frac{(k-1)}{99} \times \frac{(k-2)}{98}$ for values of k other than 93 scores M1M0A0 Correct working but then multiplied or divided by some factor scores M1M0A0 ${}^{93}P_3 / {}^{100}P_3 = 0.803 {}^{93}P_3$ seen M1 divided by ${}^{100}P_3$ M1 0.803 A1 ${}^{93}C_3 / {}^{100}C_3 = 0.803$ Allow unsimplified fractional answer 778596/970200 =9269/11550
		TOTAL	8	

	SECTION	B						
Q7 (i)	Income $0 \le x \le 20$ $20 < x \le 40$ $40 < x \le 60$ $60 < x \le 100$ $100 < x \le 200$	Frequency 238 365 142 128 45	Width 20 20 20 40 100	FD 11.9 18.25 7.1 3.2 0.5		M1 for fds A1 CAO Accept any suitable unit for fd such as eg freq per £1000.		At least 4 fds correct for M1 M1 can be also be gained from freq per 10K - 119, 182.5, 71, 32, 4.5 (at least 4 correct) and A1 for all correct Accept any suitable unit for fd, eg freq per £10K, BUT NOT FD per £1000 Allow fds correct to at least one dp If fd not explicitly given, M1 A1 can be gained from
	INCORRECT D Frequency diagr MAXIMUM Thus frequency/midp	DIAGRAMS rams can get density = free oint etc gets	M0, A0, I equency × MAX M0	L0, W1, H0 width, A0L0W1H0	1000me 200	L1 linear scale and label on vertical axis W1 linear scale on horizontal axis and correct width of bars H1 height of bars	5	all heights correct (within one square) on histogram (and M1A0 if at least 4 correct) Allow restart although given fd wrong For L1, label required on vert axis in relation to first M1 mark ie fd or frequency density or if relevant freq/£10K, freq/£k etc (NOT fd/£10K) Accept f/w or f/cw (freq/width or freq/class width) Ignore horizontal label L1 can also be gained from an accurate key – may see 1 square = 36.5 or 23.8 or 14.2 For W1, must be drawn at 0, 20, 40 etc NOT 19.5 or 20.5 etc NO GAPS ALLOWED Must have linear scale. No inequality labels on their own such as 0≤I<20, 20≤I<40 etc but allow if a clear horizontal linear scale is also given. FT of heights <i>dep</i> on M1 all must agree with their fds If fds not given and one height is wrong then max M1A0L1W1H0 – visual check only (within one square) –no need to measure precisely

(ii)	$Mean = \frac{10 \times 238 + 30 \times 365 + 50 \times 142 + 80 \times 128 + 150 \times 45}{918}$ $= \frac{37420}{918} = 40.8$	M1 for midpoints M1 for midpoints ×frequencies with divisor 918 A1 CAO	3	At least three midpoints correct for M1 (seen in (ii) or in table in (i)) No marks if not using midpoints Second M1 for sight of at least 3 double pairs seen out of $10 \times 238 + 30 \times 365 + 50 \times 142 + 80 \times 128 + 150 \times$ 45 with divisor 918 Numerator = $2380+10950+7100+10240+6750$ Use of LCB or UCB for midpoints here scores 0 For answer 40.76 or 40.8 or 41 mark as B3 37420/918 o.e. scores M1M1A0 NB Accept answers seen without working in part (ii) or (iii) (from calculator) Use of 'not quite right' midpoints such as 10.5, 30.5, etc can get M0M1A0 here and SC3 in (iii) Watch for incorrect method 238/10+365/30+142/50+128/80+45/150=40.71 Allow max 4 sf in final answer Also accept £40760, £40800 etc
(iii)	$\sum fx^2 = 238 \times 10^2 + 365 \times 30^2 + 142 \times 50^2 + 128 \times 80^2 + 45 \times 150^2$ = 2539000 Or 238 × 100 + 365 × 900 + 142 × 2500 + 128 × 6400 + 45 × 22500 = 2539000 Or 2380 × 10 + 10950 × 300 + 7100 × 50 + 10240 × 80 + 13500 × 150 = 2539000 S _{xx} = 2539000 - $\frac{37420^2}{918}$ = 1013666 s = $\sqrt{\frac{1013666}{917}}$ = 33.2	M1 for at least 3 multiples fx^2 A1 for Σfx^2 M1 for attempt at S_{xx} Dep on first M1 BUT NOTE M1M0 if their $S_{xx} < 0$ A1 CAO If using LCB or UCB	4	For A1, all midpoints and frequencies correct Or Sxx = 2539000 - 918 × 40.76 ² = 1013855, s=33.25. Using mean 40.8 leads to 1010861, s= 33.20, Using mean = 41 leads to Sxx = 995844 and s = 32.95 M1M1 for $\sum f(x-xbar)^2$ M1 for first three terms, M1 for all 5 terms 238 × (10-40.76) ² + 365 × (30-40.76) ² + 142 × (50- 40.76) ² + 128 × (80-40.76) ² + 45 × (150-40.76) ² (= 1013666) A1 for Sxx = 1013666 A1 for final answer

		consistently then allow SC2 if working is fully correct but SC0 otherwise but no marks in part (ii)		For answer 33.25 or 33.3 or 33.2 (www) can just mark as B4 - these may be from calculator without working Allow 33 with correct working rmsd = $\sqrt{(1013666/918)}$ (=33.23) gets M1A1M1A0 (if seen) WATCH FOR DIVISOR OF 918 Allow max 4 sf in final answer Allow £33200 etc
(iv)	$(\bar{x} - 2s = 40.76 - 2 \times 33.25 = -25.74)$ $\bar{x} + 2s = 40.76 + 2 \times 33.25 = 107.26$ Comment that there are almost certainly some outliers.	M1 for $\bar{x} + 2s$ or $\bar{x} - 2s$ A1 for 107.26 (FT)	4	FT any positive mean and positive sd for M1 Only follow through numerical values, not variables such as <i>s</i> , so if a candidate does not find <i>s</i> but then writes here 'limit is $40.76+2 \times$ standard deviation', do NOT award M1 (This rule of not following through variables applies in all situations)
	Appropriate comment such as 'No, since there is nothing to indicate that these high earners represent a separate population.'	E1 E1 Dep on upper limit in range 106 - 108		Award E0E0 if their upper limit > 200 Allow 'Must be some outliers' Allow any comments that implies that there are outliers No marks in (iv) unless using $\overline{x} + 2s$ or $\overline{x} - 2s$
(v)	New mean = $1.15 \times 40.76 = 46.87$ New variance = $1.15^2 \times 33.25^2 = 1462$ For misread 1.5 in place of 1.15 For $1.5 \times 40.76 = 61.1$ and $1.5^2 \times 33.25^2 = 2490$ allow SC2 if all present but SC0 otherwise	B1 FT M1A1 FT	3	FT their mean (if given to ≥ 2 s.f.) FT their s (if given to ≥ 2 s.f.) provided their s>0 If RMSD found in part (i) rather than s, then FT their RMSD For new SD = 38.24 found instead of variance give M1A0 even if called variance (and FT their s) M0A0 for 1.15 x 33.25 ² = 1271 Allow max 4 sf in final answers Min 2 sf If candidate 'starts again' only award marks for CAO
		TOTAL	19	

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Q8 (i)	$E(X) = np = 12 \times 0.2 = 2.4$ Do not allow subsequent rounding.	M1 for product A1 CAO	2	If wrong <i>n</i> used consistently throughout, allow M marks only. NB If they round to 2, even if they have obtained 2.4 first they get M1A0. For answer of '2.4 or 2 if rounded up' allow M1A0 Answer of 2 without working gets M0A0. If they attempt $E(X)$ by summing products <i>xp</i> give no marks unless answer is fully correct.
(ii)	X ~ B(12, 0.2) (A) P(Wins exactly 2) = $\binom{12}{2} \times 0.2^2 \times 0.8^{10} = 0.2835$ OR from tables 0.5583 - 0.2749 = 0.2834	M1 $0.2^2 \times 0.8^{10}$ M1 $\binom{12}{2} \times p^2 q^{10}$ A1 CAO OR: M2 for 0.5583 – 0.2749 A1 CAO	3	With $p + q = 1$ Also for 66 × 0.004295 Allow answers within the range 0.283 to 0.284 with or without working or 0.28 to 0.283 if working shown See tables at the website http://www.mei.org.uk/files/pdf/formula_book_mf2.pd f
	(B) P(Wins at least 2) = 1-0.2749 = 0.7251	M1 P(X≤1) M1 1-P(X≤1) A1 CAO	3	M1 0.2749 seen M1 1 – 0.2749 seen Allow 0.725 to 0.73 but not 0.72. Point probability method: P(1) = $12 \times 0.2 \times 0.8^{11} = 0.2062$, P(0) = $0.8^{12} = 0.0687$ So P(X ≤ 1) = 0.2749 gets M1 then mark as per scheme SC1 for 1 – P(X ≤ 2) = 1 – 0.5583 = 0.4417 For misread of tables value of 0.2749, allow 0 in (<i>A</i>) but MAX M1M1 in (<i>B</i>) For P(X>1) = P(X=2) + P(X=3) + P(X=4) + allow M1 for 0.2835+0.2362+0.1329+0.0532+0.0155 and second M1 for 0.0033+0.0005+0.0001 and A1 for 0.725 or better M0M0A0 for 1 - P(X=1) = 1 – 0.2062 = 0.7938
				$\frac{1}{10000000000000000000000000000000000$

Mark Scheme

	B1 for 0.0867		Allow any form of statement of CR eg $X \ge 8$, 8 to 20, 8
OR Critical region method:	B1 for 0.0321		or above, $X > 8$, $\{8,\}$, annotated number line, etc
Let $X \sim B(20, 0.2)$	M1 for at least one		but not $P(X \ge 8)$
$P(X \ge 7) = 1 - P(X \le 6) = 1 - 0.9133 = 0.0867 > 5\%$	comparison with 5%		$\{8,9,10,11,12\}$ gets max B2M1A0 – tables stop at 8.
$P(X \ge 8) = 1 - P(X \le 7) = 1 - 0.9679 = 0.0321 < 5\%$	A1 CAO for critical		NB USE OF POINT PROBABILITIES gets
	region and not		B0B0M0A0
So critical region is {8,9,10,11,12,13,14,15,16,17,18,19,20}	significant or 'accept		Use of complementary probabilities
7 door not light the critical ration so not significant	H_0 ' or 'cannot reject		Providing there is sight of 95%, allow B1 for 0.9133,
/ does not he in the critical region, so not significant,	H_0 ' or 'reject H_1 '		B1 for 0.9679, M1 for comparison with 95% A1CAO
So there is not enough avidence to reject the null hypothesis	dep on M1 and at least		for correct CR
and we conclude that there is not enough evidence to suggest	one B1		See additional notes below the scheme for other
			possibilities
that An is better at winning games than wark.	E1 dep on M1A1		PLEASE CHECK THAT THERE IS NO EXTRA
			WORKING ON THE SECOND PAGE IN THE
			ANSWER BOOKLET
	TOTAL	17	

NOTE RE OVER-SPECIFICATION OF ANSWERS

If answers are grossly over-specified (see instruction 8), deduct the final answer mark in every case, except where there are more than two overspecified answers in a single question (only likely in question 7) in which case deduct a mark in only the first two cases of over-specification in that question. Probabilities should also be rounded to a sensible degree of accuracy.

ADDITIONAL NOTES RE Q8 PART iii

Use of n = 12

 $\overline{P(X \ge 7)} = 1 - P(X \le 6) = 1 - 0.9961 = 0.0039 < 5\%$

So significant or reject H_0 etc, so there evidence to suggest that Ali is better at winning games than Mark.

Gets B1 for $P(X \ge 7)$ B1 for 0.0039 M1 for comparison with 5% dep on B1 for 0.0039 A1 for significant E1 for evidence to suggest that Ali is better at winning games than Mark. Then award MR -1 so maximum of 4 possible

Comparison with 95% method

B1 for $P(X \le 6)$ B1 for 0.9133

M1 for comparison with 95% dep on B1 A1 for not significant or 'accept H_0 ' or 'cannot reject H_0 ' E1

Smallest critical region method:

Either:

Smallest critical region that 7 could fall into gets B1 and has size 0.0867 gets B1, This is > 5% gets M1, A1, E1 as per scheme NB These marks only awarded if 7 used, not other values.

Use of *k* method with no probabilities quoted:

 $P(X \ge 7) = 1 - P(X \le 6) > 5\%$ $P(X \ge 8) = 1 - P(X \le 7) < 5\%$ These may be seen in terms of *k* or *n*. Either k = 8 or k - 1 = 7 so k = 8 gets SC1 so CR is {8,9,10,11,12,13,14,15, 16, 17, 18, 19, 20} gets another SC1 and conclusion gets another SC1

Use of *k* method with one probability quoted:

1 - 0.9679 < 5% or 0.0321 < 5% gets B0B1M1 $P(X \le k - 1) = P(X \le 7)$ so k - 1 = 7 so k = 8 (or just k = 8) so CR is {8,9,10,11,12,13,14,15, 16, 17, 18, 19, 20} and conclusion gets A1E1

Two tailed test with H₁: $p \neq 0.2$ Hyp gets max B1B1B0E0 $P(X \ge 7) = 0.0867$ gets B1B1comparison with 2.5% gets M1 (must be 2.5%) Final marks A0E0

<u>Two tailed test done but with correct H₁: p>0.2</u> Hyp gets max B1B1B1E1

Mark Scheme

<u>if compare with 5%</u> ignore work on lower tail and mark upper tail as per scheme so can score full marks <u>if compare with 2.5%</u> no marks B0B0M0A0E0

<u>One tailed test with $H_1: p < 0.2$ </u> Hyp gets max B1B1B0E0 no further marks B0B0M0A0E0

<u>Lower tailed test with $H_1: p > 0.2$ </u> Hyp gets max B1B1B0E0 no further marks B0B0M0A0E0

Line diagram method

B1 for squiggly line between 7 and 8 or on 8 exclusively (ie just one line), B1*dep* for arrow pointing to right, M1 0.0321 seen on diagram from squiggly line or from 8, A1E1 for correct conclusion

Bar chart method

B1 for line clearly on boundary between 7 and 8 or within 8 block exclusively (ie just one line), B1*dep* for arrow pointing to right, M1 0.0321 seen on diagram from boundary line or from 8, A1E1 for correct conclusion

Using P(Not faulty) method

 $H_0: p=0.8$, $H_1: p<0.8$, where p represents the prob that Ali loses a game Ali claims that the proportion of games that he loses is less than 80% gets B1B1B1E1

 $P(X \le 13) = 0.0867 > 5\%$ So not significant, so there is not enough evidence to reject the null hypothesis and we conclude that there is not enough evidence to suggest that Ali is better at winning games than Mark. Gets B1B1M1A1E1

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