

# ADVANCED SUBSIDIARY GCE MATHEMATICS (MEI)

4751

Introduction to Advanced Mathematics (C1)

#### **QUESTION PAPER**

Candidates answer on the printed answer book.

#### **OCR** supplied materials:

- Printed answer book 4751
- MEI Examination Formulae and Tables (MF2)

#### Other materials required:

None

## Monday 10 January 2011 Morning

**Duration:** 1 hour 30 minutes

#### **INSTRUCTIONS TO CANDIDATES**

These instructions are the same on the printed answer book and the question paper.

- The question paper will be found in the centre of the printed answer book.
- Write your name, centre number and candidate number in the spaces provided on the printed answer book.
   Please write clearly and in capital letters.
- Write your answer to each question in the space provided in the printed answer book. Additional paper
  may be used if necessary but you must clearly show your candidate number, centre number and question
  number(s).
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer all the questions.
- Do not write in the bar codes.
- You are **not** permitted to use a calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

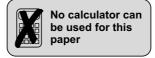
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- The number of marks is given in brackets [] at the end of each question or part question on the question paper.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is 72.
- The printed answer book consists of 12 pages. The question paper consists of 4 pages. Any blank pages are indicated.

#### **INSTRUCTION TO EXAMS OFFICER / INVIGILATOR**

• Do not send this question paper for marking; it should be retained in the centre or destroyed.



#### Section A (36 marks)

- Find the equation of the line which is parallel to y = 5x 4 and which passes through the point (2, 13). Give your answer in the form y = ax + b.
- 2 (i) Write down the value of each of the following.

(A) 
$$4^{-2}$$

(B) 
$$9^0$$

- (ii) Find the value of  $\left(\frac{64}{125}\right)^{\frac{4}{3}}$ . [2]
- 3 Simplify  $\frac{(3xy^4)^3}{6x^5y^2}$ . [3]
- 4 Solve the inequality 5 2x < 0. [2]
- 5 The volume V of a cone with base radius r and slant height l is given by the formula

$$V = \frac{1}{3}\pi r^2 \sqrt{l^2 - r^2}.$$

[4]

Rearrange this formula to make *l* the subject.

- 6 Find the first 3 terms, in ascending powers of x, of the binomial expansion of  $(2-3x)^5$ , simplifying each term.
- 7 (i) Express  $\frac{81}{\sqrt{3}}$  in the form  $3^k$ . [2]

(ii) Express 
$$\frac{5+\sqrt{3}}{5-\sqrt{3}}$$
 in the form  $\frac{a+b\sqrt{3}}{c}$ , where  $a,b$  and  $c$  are integers. [3]

8 Find the coordinates of the point of intersection of the lines x + 2y = 5 and y = 5x - 1. [3]

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9 Fig. 9 shows a trapezium ABCD, with the lengths in centimetres of three of its sides.

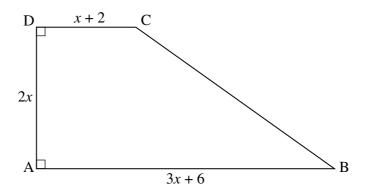


Fig. 9

This trapezium has area 140 cm<sup>2</sup>.

(i) Show that 
$$x^2 + 2x - 35 = 0$$
. [2]

(ii) Hence find the length of side AB of the trapezium. [3]

10 Select the best statement from

 $P \Rightarrow Q$ 

 $P \Leftarrow Q$ 

 $P \Leftrightarrow Q$ 

none of the above

to describe the relationship between P and Q in each of the following cases.

(i) P: WXYZ is a quadrilateral with 4 equal sides

Q: WXYZ is a square

(ii) P: n is an odd integer

Q:  $(n+1)^2$  is an odd integer

(iii) P: n is greater than 1 and n is a prime number

Q: 
$$\sqrt{n}$$
 is not an integer

[3]

#### **Section B** (36 marks)

11 The points A (-1, 6), B (1, 0) and C (13, 4) are joined by straight lines.

(i) Prove that the lines AB and BC are perpendicular.

[3]

(ii) Find the area of triangle ABC.

[3]

(iii) A circle passes through the points A, B and C. Justify the statement that AC is a diameter of this circle. Find the equation of this circle. [6]

(iv) Find the coordinates of the point on this circle that is furthest from B.

[1]

**12** (i) You are given that f(x) = (2x - 5)(x - 1)(x - 4).

(A) Sketch the graph of 
$$y = f(x)$$
. [3]

(B) Show that 
$$f(x) = 2x^3 - 15x^2 + 33x - 20$$
. [2]

(ii) You are given that  $g(x) = 2x^3 - 15x^2 + 33x - 40$ .

(A) Show that 
$$g(5) = 0$$
. [1]

- (B) Express g(x) as the product of a linear and quadratic factor. [3]
- (C) Hence show that the equation g(x) = 0 has only one real root. [2]
- (iii) Describe fully the transformation that maps y = f(x) onto y = g(x). [2]

13

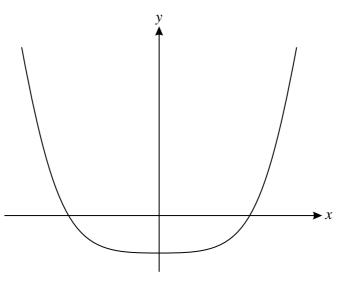


Fig. 13

Fig. 13 shows the curve  $y = x^4 - 2$ .

- (i) Find the exact coordinates of the points of intersection of this curve with the axes. [3]
- (ii) Find the exact coordinates of the points of intersection of the curve  $y = x^4 2$  with the curve  $y = x^2$ .
- (iii) Show that the curves  $y = x^4 2$  and  $y = kx^2$  intersect for all values of k. [2]



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Candidate forename				Candidate surname			
Centre number				Candidate n	umber		

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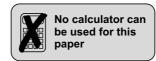
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## Section A (36 marks)

1	
<b>2</b> (i) (A)	
<b>2</b> (i) (B)	
2 (ii)	
2	
3	

4	
5	
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7 (i)	
7 (ii)	
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9 (i)	
9 (ii)	
10 (i)	
10 (ii)	
10 (iii)	

## Section B (36 marks)

11 (i)	
11 (ii)	

11 (iii)	
11 (iv)	

<b>12(i)</b> (A)	
<b>12</b> (i)( <i>B</i> )	
<b>.</b>	
<b>12(ii)</b> (A)	

<b>12(ii)</b> (B)	
<b>12</b> ( <b>ii</b> )( <i>C</i> )	
12 (iii)	

13 (i)	
13 (ii)	

13 (iii)	

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