

1)



i)  $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 30 \cos 45^\circ \times t \\ 30 \sin 45^\circ \times t - 4.9t^2 \end{pmatrix}$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 21.2t \\ 21.2t - 4.9t^2 \end{pmatrix}$$

ii)  $x = 21.2t \Rightarrow t = \frac{x}{21.2}$

Subst gives

$$y = \frac{21.2x}{21.2} - \frac{4.9x^2}{21.2^2}$$

$$y = x - 0.0109x^2$$

$$y = x - 0.011x^2$$

iii) When  $x = 10$

$$y = 10 - 0.011 \times 100$$

$$y = 8.9$$

iv) When  $y = 20$

$$20 = x - 0.011x^2$$

$$0.011x^2 - x + 20 = 0$$

From graphics calculator

$$x = 29.7 \text{ or } 61.2$$

2)



At time  $t$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 10 \cos 14^\circ \times t \\ 10 \sin 14^\circ \times t - 4.9t^2 + 1.5 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 9.703t \\ 2.419t - 4.9t^2 + 1.5 \end{pmatrix}$$

$$x = 9.703t \Rightarrow t = \frac{x}{9.703}$$

Subst gives

$$y = 2.419 \times \frac{x}{9.703} - \frac{4.9x^2}{9.703^2} + 1.5$$

$$y = 1.5 + 0.25x - 0.052x^2$$

ii)

At top of wicket  $y = 0.7$

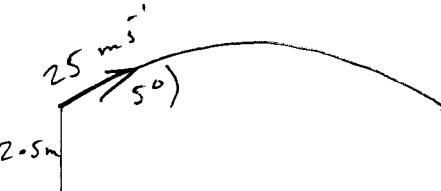
$$0.7 = 1.5 + 0.25x - 0.053x^2$$

$$0.053x^2 - 0.25x - 0.8 = 0$$

From graphics calculator

$$x = 6.9 \text{ m}$$

3)



At time  $t$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 25 \cos 5^\circ \times t \\ 2.5 + 25 \sin 5^\circ \times t - 4.9t^2 \end{pmatrix}$$

## MEI MECHANICS 1

## PROJECTILES

## EXERCISE 6E

$$3 \text{ cont}) \quad \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 24.9t \\ 2.5 + 2.18t - 4.9t^2 \end{pmatrix} \quad x = 0.819ut \Rightarrow t = \frac{x}{0.819u}$$

$$x = 24.9t \Rightarrow t = \frac{x}{24.9}$$

Subst gives

$$y = 2.5 + 2.18 \frac{x}{24.9} - \frac{4.9}{24.9} x^2$$

$$y = 2.5 + 0.0876x - 0.0079x^2 \quad \text{ii)}$$

ii) Ball lands when  $y = 0$ 

$$0 = 2.5 + 0.0876x - 0.0079x^2$$

From calculator

$$x = 24.1 \text{ m}$$

iii)

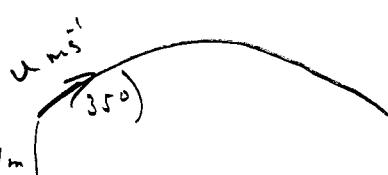
When  $x = 12$ 

$$y = 2.5 + 0.087 \times 12 - 0.0079 \times 12^2$$

$$y = 2.4064 \text{ m}$$

Yes it clears the 1m high net

4)

At time  $t$ 

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} u \cos 35^\circ \times t \\ 1 + u \sin 35^\circ \times t - 4.9t^2 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0.819ut \\ 1 + 0.574ut - 4.9t^2 \end{pmatrix}$$

iii)

To land in court

$$y \leq 0 \text{ when } x = 3 + 5 = 8$$

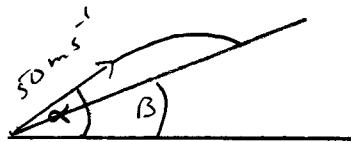
$$0 \geq 1 + 0.7 \times 8 - \frac{7.45 \times 8^2}{u^2}$$

$$\frac{476.8}{u^2} \geq 6.6$$

$$\frac{476.8}{6.6} \geq u^2 \Rightarrow u \leq 8.5 \text{ m}$$

10)

i)



$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 50 \cos \alpha \cdot t \\ 50 \sin \alpha \cdot t - 4.9t^2 \end{pmatrix}$$

$$\sin \alpha = \frac{4}{5} \Rightarrow \cos \alpha = \frac{3}{5}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 30t \\ 40t - 4.9t^2 \end{pmatrix}$$

$$x = 30t \Rightarrow t = \frac{x}{30}$$

Subst in y

$$y = \frac{40x}{30} - 4 \frac{9x^2}{900}$$

$$y = \frac{4x}{3} - \frac{x^2}{180}$$

ii)

$\tan \beta$  is gradient of slope  
line passes through origin

$$\therefore y = \frac{1}{2}x + 0 = \frac{1}{2}x$$

iii)

Using answer from book

$$y = \frac{4x}{3} - \frac{x^2}{180}$$

Subst  $\frac{1}{2}x$  for y

$$\frac{x}{2} = \frac{4x}{3} - \frac{x^2}{180}$$

 $\times 180$ 

$$90x = 240x - x^2$$

$$x^2 - 150x = 0$$

$$x(x - 150) = 0$$

H.T.S slope when  $x = 150$   
 $y = 75$

At point  $(150, 75)$ 

iv) Range  $= \sqrt{150^2 + 75^2}$   
 $= 167.7 \text{ m}$

v)  $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 50 \cos 45^\circ \cdot t \\ 50 \sin 45^\circ \cdot t - 5t^2 \end{pmatrix}$

Taking  $g = -10 \text{ m s}^{-2}$  as book does

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 35.36t \\ 35.36t - 5t^2 \end{pmatrix}$$

$$\Rightarrow y = \frac{35.36x}{35.36} - \frac{5x^2}{35.36^2}$$

$$y = x - \frac{5x^2}{35.36^2}$$

Subst  $\frac{1}{2}x$  for y

$$\frac{x}{2} = x - \frac{5x^2}{35.36^2}$$

$$\frac{5x^2}{35.36^2} - \frac{x}{2} = 0$$

$$10x^2 - 1250x = 0$$

$$x^2 - 125x = 0$$

$$\Rightarrow x = 0 \text{ or } x = 125$$

H.T.S at point  $(125, 62.5)$ Range up slope  $= \sqrt{125^2 + 62.5^2}$ 

$$= 140 \text{ m}$$

vi) No since  $140 < 167.7 \text{ m}$