

MEI MECHANICS 2

IMPULSE

EXERCISE 6A

$$\text{i)} 50 \text{ kg} \times 10 \text{ ms}^{-1} = 500 \text{ kgms}^{-1}$$

$$\text{ii)} 5000 \text{ kg} \times 4 \text{ ms}^{-1} = 20000 \text{ kgms}^{-1}$$

$$\text{iii)} 7000 \times 10^3 \text{ kg} \times 40 \text{ ms}^{-1} = 2.8 \times 10^8 \text{ kgms}^{-1}$$

$$\text{iv)} 2 \times 10^{-19} \text{ kg} \times 1 \times 10^{-3} \text{ ms}^{-1} = 2 \times 10^{-22} \text{ kgms}^{-1}$$

2)

i) Impulse = change in momentum

$$1.3 \times 10^3 \text{ kg} \times 14 \text{ ms}^{-1} = 18200 \text{ Ns}$$

$$\text{ii)} 1.5 \times 10^{-3} \text{ kg} \times 1.5 \text{ ms}^{-1} = 2.25 \times 10^{-3} \text{ Ns}$$

$$\text{iii)} 0.15 \text{ kg} \times 20 \text{ ms}^{-1} = 3 \text{ Ns}$$

$$\text{iv)} 25 \times 10^{-3} \text{ kg} \times 400 \text{ ms}^{-1} = 10 \text{ Ns}$$

3)

$$\text{i)} F = mg = 1.5 \times 10 = 15 \text{ N}$$

$$\text{ii)} s = ut + \frac{1}{2}at^2$$

$$s = 0 + \frac{1}{2} \times 10 \times 2^2 = 20 \text{ m}$$

$$\text{iii)} v = u + at = 0 + 10 \times 2 = 20 \text{ ms}^{-1}$$

$$\text{iv)} F_s = 15 \times 20 = 300 \text{ J}$$

Work done by gravitational force

Converts gpe to k.e.

$$\frac{1}{2}mv^2 = \frac{1}{2} \times 1.5 \times 20^2 = 300 \text{ J}$$

$$\text{v)} Ft = 15 \times 2 = 30 \text{ Ns}$$

= change in momentum

$$= mv - mu$$

$$= 1.5 \times 20 - 0 = 30 \text{ Ns}$$

4)

$$\text{i)} mv = 0.06 \text{ kg} \times 20 \text{ ms}^{-1} \\ = 1.2 \text{ kgms}^{-1}$$

$$\text{ii)} \text{At top } v = u + at \\ v = 0, \quad 0 = 20 - 10t$$

$$\Rightarrow t = 2 \text{ s}$$

$$\text{iii)} \text{At top } mv = 0 \text{ kgms}^{-1}$$

$$\text{iv)} \text{Impulse} = \text{change in momentum} \\ \therefore = 1.2 \text{ kgms}^{-1} \text{ or } 1.2 \text{ Ns}$$

5)

i) Impulse = change in momentum reqd

$$= 0.425 \text{ kg} \times 5 \text{ ms}^{-1}$$

$$= 2.125 \text{ Ns}$$

ii)

$$\text{a)} Ft = 2.125$$

$$F = \frac{2.125}{t}$$

$$F = \frac{2.125}{0.1} = 21.25 \text{ N}$$

b)

$$F = \frac{2.125}{0.05} = 42.5 \text{ N}$$

iii) Same impulse required but longer time therefore smaller force required since

$$Ft = \text{Impulse}$$

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6) i) Impulse = Change in momentum
 $= 0.9 \times 10^3 \text{ kg} \times 13.2 \text{ ms}^{-1}$
 $= 11880 \text{ Ns}$

ii) $Ft = \text{Impulse}$
 $F = \frac{\text{Impulse}}{t} = \frac{11880}{0.12}$
 $F = 99000 \text{ N}$

iii) $F = ma$
 $a = \frac{F}{m} = \frac{99000}{900}$
 $a = 110 \text{ ms}^{-2} = 11g$

iv) For a given collision the impulse is fixed. However, by extending the time of the impact, the average force can be reduced.

7) i) $v^2 = u^2 + 2as$
 $v^2 = 0 + 2 \times 9.8 \times 1.5$
 $v^2 = 29.4$
 $v = 5.42 \text{ ms}^{-1}$

ii) Impulse = change in momentum
 $= mv = 20 \text{ kg} \times 5.42 \text{ ms}^{-1}$
 $= 108.4 \text{ Ns}$

iii) Equal and opposite impulse = 108.4 Ns

iv) $Ft = J$
 $F = \frac{J}{t} = \frac{108.4}{0.2}$

Average force $F = 542 \text{ N}$

8) i) $\xrightarrow{\text{+ve direction}}$
 $mv = 10 \times 10^3 \text{ kg} \times 3 \text{ ms}^{-1}$
 $= 3.0 \times 10^4 \text{ kg ms}^{-1}$

ii) $mv = 10 \times 10^3 \text{ kg} \times -1.5 \text{ ms}^{-1}$
 $= -1.5 \times 10^4 \text{ kg ms}^{-1}$

i.e. in opposite direction to original

iii) Impulse = change in momentum
 $= -1.5 \times 10^4 - 3.0 \times 10^4$
 $= -4.5 \times 10^4 \text{ Ns}$

- sign indicates direction of impulse is in opposite direction to original motion.

iv) Area under graph represents impulse or change in momentum

v) $|J| = 45000 \text{ Ns}$
Area of $\Delta = \frac{1}{2} \text{ base} \times \text{height}$
 $\frac{1}{2} \times 0.2 \times h = 45000$

$\Rightarrow h = 450,000 \text{ N} = 7.5 \times F$

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9)

i)

$$\text{i) } \underline{J} = m\underline{v} - m\underline{u}$$

$$\underline{J} = m(\underline{v} - \underline{u})$$

$$-4.8\hat{i} + 1.2\hat{j} = 0.15(\underline{v} - (12\hat{i} - 8\hat{j}))$$

$$\begin{pmatrix} -4.8 \\ 1.2 \end{pmatrix} = 0.15 \begin{pmatrix} v_1 - 12 \\ v_2 + 8 \end{pmatrix}$$

$$\begin{pmatrix} -4.8 \\ 1.2 \end{pmatrix} = \begin{pmatrix} v_1 - 12 \\ v_2 + 8 \end{pmatrix}$$

$$\begin{pmatrix} v_1 \\ v_2 \end{pmatrix} = \begin{pmatrix} -32 + 12 \\ 8 - 8 \end{pmatrix} = \begin{pmatrix} -20 \\ 0 \end{pmatrix}$$

$$\underline{v} = -20\hat{i}$$

Before

$$\underline{u} = 3.5 \cos 60\hat{i} - 3.5 \sin 60\hat{j}$$



$$\underline{u} = 1.75\hat{i} - 1.75\sqrt{3}\hat{j}$$

After

$$\underline{v} = 2 \cos 30\hat{i} + 2 \sin 30\hat{j}$$

$$\underline{v} = \sqrt{3}\hat{i} + \hat{j}$$

iv)

Impulse = change in momentum

$$= m\underline{v} - m\underline{u}$$

$$= m(v - u)$$

$$= 0.08(\sqrt{3}\hat{i} + \hat{j} - (1.75\hat{i} - 1.75\sqrt{3}\hat{j}))$$

$$= 0.08(-0.0179\hat{i} + 4.031\hat{j})$$

$$= -1.432 \times 10^{-3}\hat{i} + 0.322\hat{j}$$

↑ Change in momentum

(x)

$$\alpha = \tan^{-1} \frac{0.322}{1.432 \times 10^{-3}} = 89.7^\circ$$

Hardly any change in momentum parallel to cushion

10)

i)

$$\underline{J} = m(\underline{v} - \underline{u})$$

$$-4.8\hat{i} + 1.2\hat{j} = 0.15(\underline{v} - (12\hat{i} - 8\hat{j}))$$

$$\begin{pmatrix} -4.8 \\ 1.2 \end{pmatrix} = 0.15 \begin{pmatrix} v_1 - 12 \\ v_2 + 8 \end{pmatrix}$$

$$\begin{pmatrix} -4.8 \\ 1.2 \end{pmatrix} = \begin{pmatrix} v_1 - 12 \\ v_2 + 8 \end{pmatrix}$$

$$\begin{pmatrix} v_1 \\ v_2 \end{pmatrix} = \begin{pmatrix} -32 + 12 \\ 8 - 8 \end{pmatrix} = \begin{pmatrix} -20 \\ 0 \end{pmatrix}$$

$$\underline{v} = -20\hat{i}$$

ii)

$$\underline{J} = m\underline{v} - m\underline{u}$$

$$\underline{J} = 0.15(\underline{v} - \underline{u})$$

$$\underline{J} = 0.15 \left(\begin{pmatrix} 14 \\ 4 \\ 3 \end{pmatrix} - \begin{pmatrix} -20 \\ 0 \\ 0 \end{pmatrix} \right)$$

$$\underline{J} = 0.15 \begin{pmatrix} 34 \\ 4 \\ 3 \end{pmatrix}$$

$$\underline{J} = \begin{pmatrix} 5.1 \\ 0.6 \\ 0.45 \end{pmatrix}$$

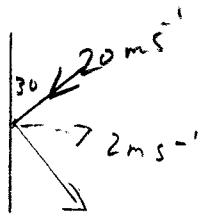
$$\underline{J} = 5.1\hat{i} + 0.6\hat{j} + 0.45\hat{k}$$

$$|J_1| = \sqrt{(-4.8)^2 + 1.2^2} = 4.95 \text{ NS}$$

$$|J_2| = \sqrt{5.1^2 + 0.6^2 + 0.45^2} = 5.15 \text{ NS}$$

2nd player Fatima hits harder

- 11) i) Vertical component of velocity unchanged



Horizontal component of velocity changed by $20 \sin 30 + 2$
 $= 12 \text{ ms}^{-1}$

Change in momentum

$$4 \times 10^3 \text{ kg} \times 12 \text{ ms}^{-1} \\ = 0.048 \text{ kg ms}^{-1}$$

Impulse of window on hailstone

a) $= 0.048 \text{ Ns}$
 at 90° to window \rightarrow

Impulse of hailstone on window

b) $= 0.048 \text{ Ns}$
 at 90° to window \leftarrow

ii)
 Hailstones 540 per min
 $\approx 9 \text{ per second}$

Impulse $= 9 \times 0.048 = 0.432 \text{ N}$
 per second

\therefore Average Force $= 0.432 \text{ N}$

12)

i) Area under graph = impulse or change in momentum.

ii) Total impulse

$$= \frac{1}{2} \times 1 \times 2500 + \frac{1}{2} (2500 + 3500) \times 1$$

$$+ \frac{1}{2} (3500 + 4500) \times 2$$

$$= 1250 + 3000 + 8000 \text{ Ns}$$

$$= 12250 \text{ Ns}$$

iii)

Impulse = change in momentum

$$mV - mu = 12250$$

$$2500V - 0 = 12250$$

$$V = 4.9 \text{ ms}^{-1}$$

H